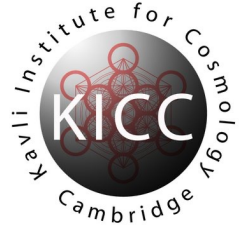




UNIVERSITY OF  
CAMBRIDGE



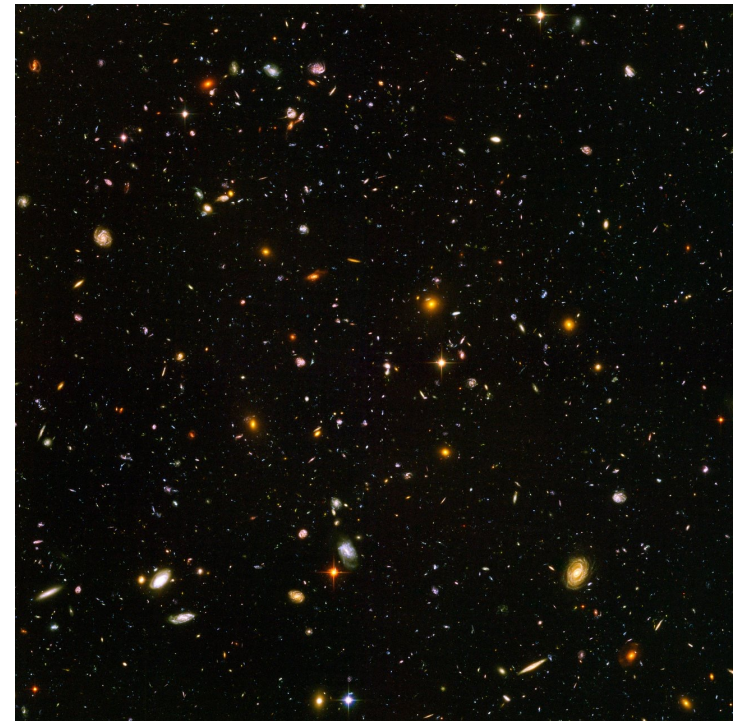
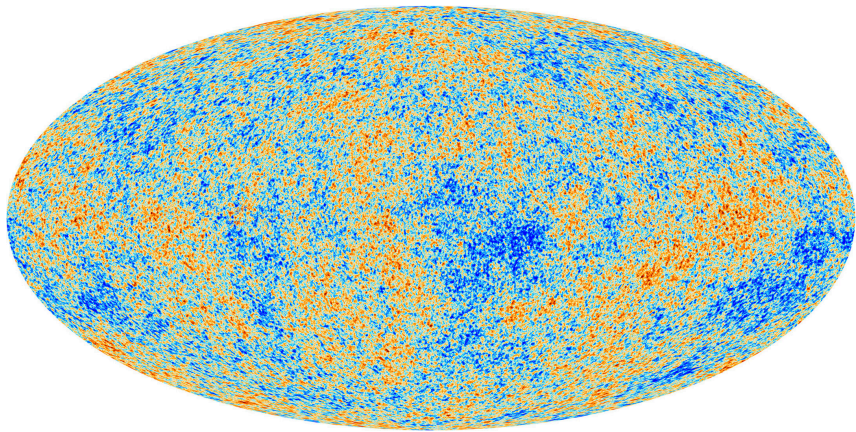
# Formation of Structure in the Universe

Lent Term 2023

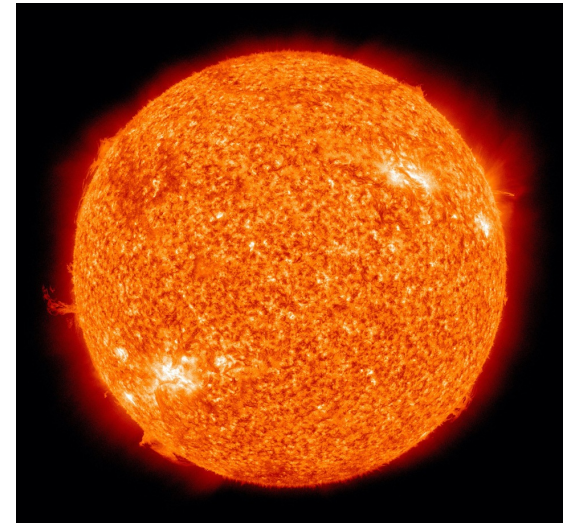
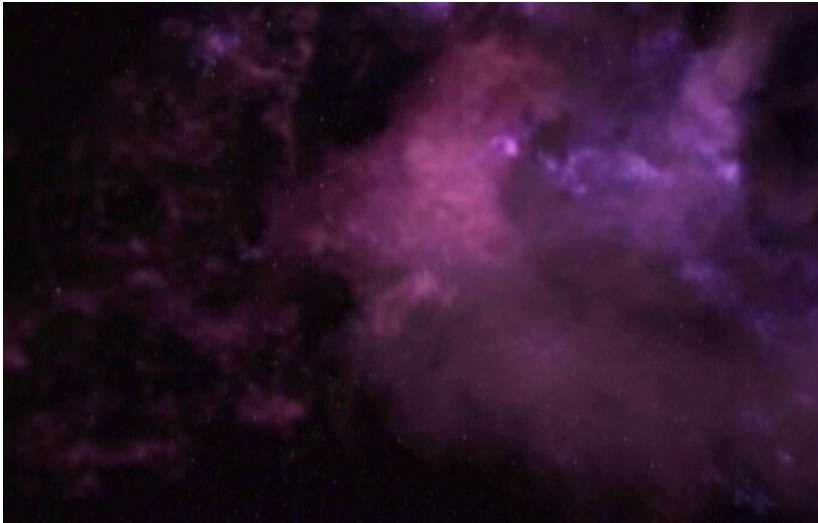
Dr. Nicolas Laporte – Kavli Institute for Cosmology

[nl408@cam.ac.uk](mailto:nl408@cam.ac.uk) – Office K32

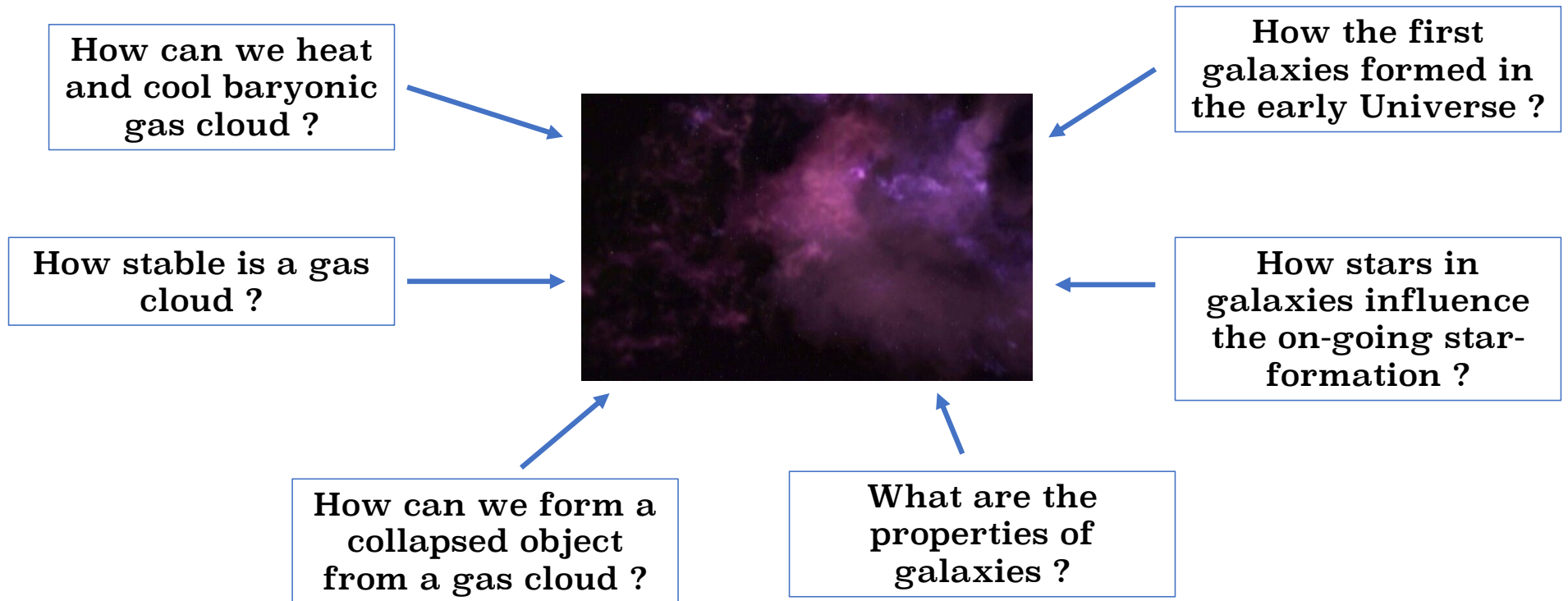
# Formation of Structure in the Universe in a nutshell



# Formation of Structure in the Universe in a nutshell



# Formation of Structure in the Universe in a nutshell





# Formation of Structure in the Universe in a nutshell

Date	Topic	Date	Topic	Date	Topic
23/01/2023	Introduction	13/02/2023	From gas cloud to collapsed object	06/03/2023	Gravitational instabilities in the cosmological context
27/01/2023	Physical process in baryonic gas (part 1)	17/02/2023	Galaxies and star-formation on galactic scales (part 1)	10/03/2023	Hierarchical structure formation (part 1)
30/01/2023	Physical process in baryonic gas (part 2)	20/02/2023	Galaxies and star-formation on galactic scales (part 2)	13/03/2023	Hierarchical structure formation (part 2)
03/02/2023	Gravitational stability and instability (part 1)	24/02/2023	Galaxies and star-formation on galactic scales (part 3)	17/03/2023	Galaxy formation and evolution
<del>06/02/2023</del>	Gravitational stability and instability (part 2)	27/02/2023	Feedback processes in star formation	April 2023	Exam
10/02/2023	Gravitational collapse	03/03/2023	Galaxies interaction and triggering star-formation		

# Supervision

**3 groups :**

- 6-8 students/group
- please sign in (*email circulating soon*)
- 3 sessions

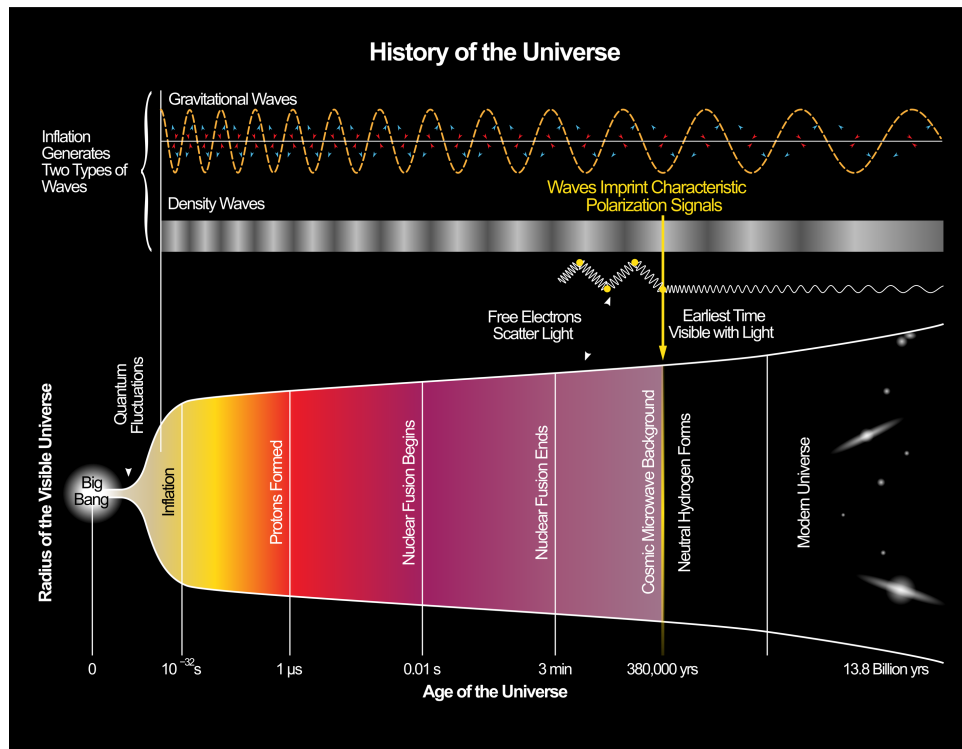
Group ID	Session 1		Session 2		Session 3	
	Date	Room	Date	Room	Date	Room
<b>1</b>						
<b>2</b>						
<b>3</b>						



# Introduction

## Chapter 1

# The first 3 minutes of the Universe



$t=0$ s : the Big-Bang

$t=10^{-36}$  to  $t=10^{-32}$ s : inflation

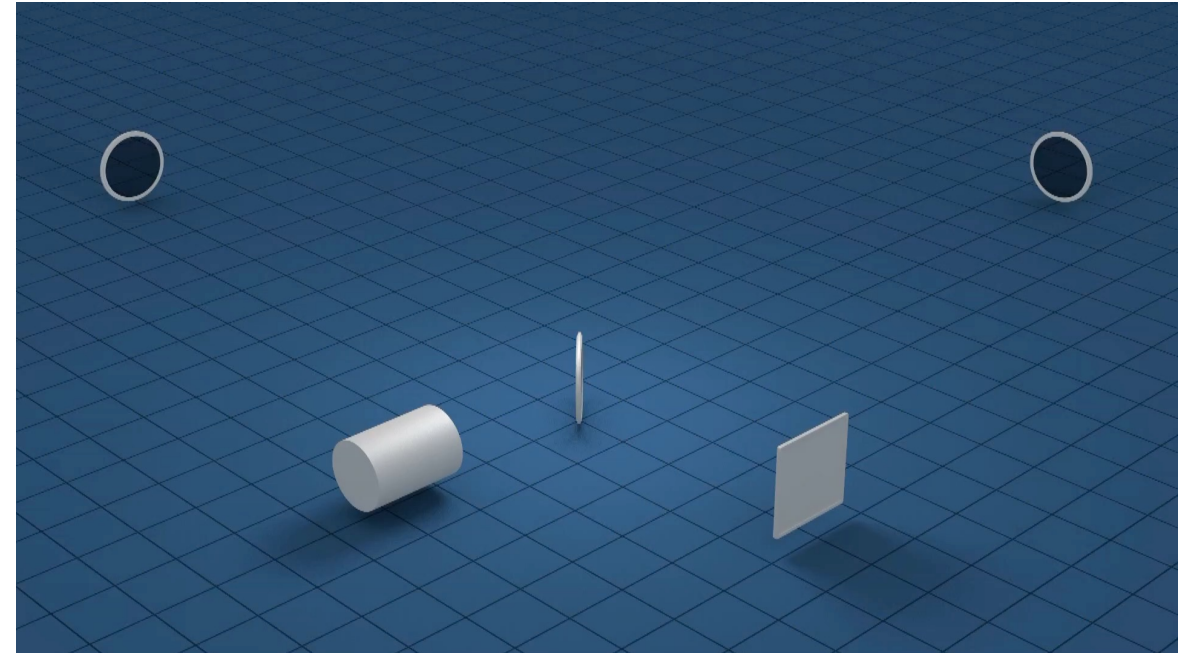
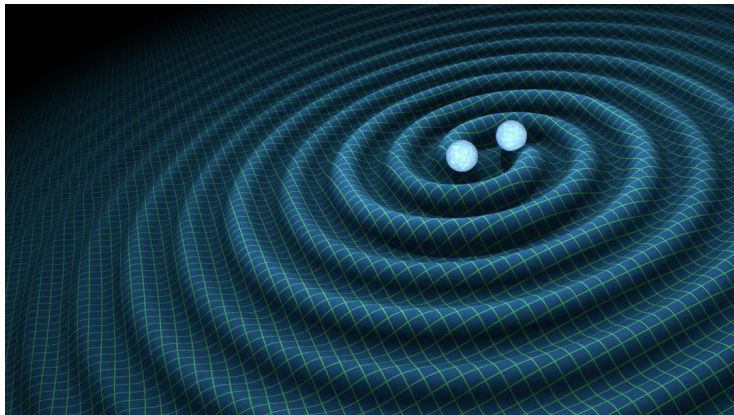
- emission of gravitational waves
- emission of density waves

Guzzetti et al. 2016, arXiv: 1605.01615

three generations of matter (fermions)			interactions / force carriers (bosons)	
I	II	III		
mass $\approx 2.2 \text{ MeV}/c^2$ charge $\frac{2}{3}$ spin $\frac{1}{2}$ <b>u</b> up	mass $\approx 1.28 \text{ GeV}/c^2$ charge $\frac{2}{3}$ spin $\frac{1}{2}$ <b>c</b> charm	mass $\approx 173.1 \text{ GeV}/c^2$ charge $\frac{2}{3}$ spin $\frac{1}{2}$ <b>t</b> top	mass 0 charge 0 spin 1 <b>g</b> gluon	mass $\approx 124.97 \text{ GeV}/c^2$ charge 0 spin 0 <b>H</b> higgs
mass $\approx 4.7 \text{ MeV}/c^2$ charge $-\frac{1}{3}$ spin $\frac{1}{2}$ <b>d</b> down	mass $\approx 96 \text{ MeV}/c^2$ charge $-\frac{1}{3}$ spin $\frac{1}{2}$ <b>s</b> strange	mass $\approx 4.18 \text{ GeV}/c^2$ charge $-\frac{1}{3}$ spin $\frac{1}{2}$ <b>b</b> bottom	mass 0 charge 0 spin 1 <b><math>\gamma</math></b> photon	<b>SCALAR BOSONS</b>
mass $\approx 0.511 \text{ MeV}/c^2$ charge -1 spin $\frac{1}{2}$ <b>e</b> electron	mass $\approx 105.66 \text{ MeV}/c^2$ charge -1 spin $\frac{1}{2}$ <b><math>\mu</math></b> muon	mass $\approx 1.7768 \text{ GeV}/c^2$ charge -1 spin $\frac{1}{2}$ <b><math>\tau</math></b> tau	mass $\approx 91.19 \text{ GeV}/c^2$ charge 0 spin 1 <b>Z</b> Z boson	
mass $< 1.0 \text{ eV}/c^2$ charge 0 spin $\frac{1}{2}$ <b><math>\nu_e</math></b> electron neutrino	mass $< 0.17 \text{ MeV}/c^2$ charge 0 spin $\frac{1}{2}$ <b><math>\nu_\mu</math></b> muon neutrino	mass $< 18.2 \text{ MeV}/c^2$ charge 0 spin $\frac{1}{2}$ <b><math>\nu_\tau</math></b> tau neutrino	mass $\approx 80.39 \text{ GeV}/c^2$ charge $\pm 1$ spin 1 <b>W</b> W boson	
<b>LEPTONS</b>			<b>GAUGE BOSONS VECTOR BOSONS</b>	



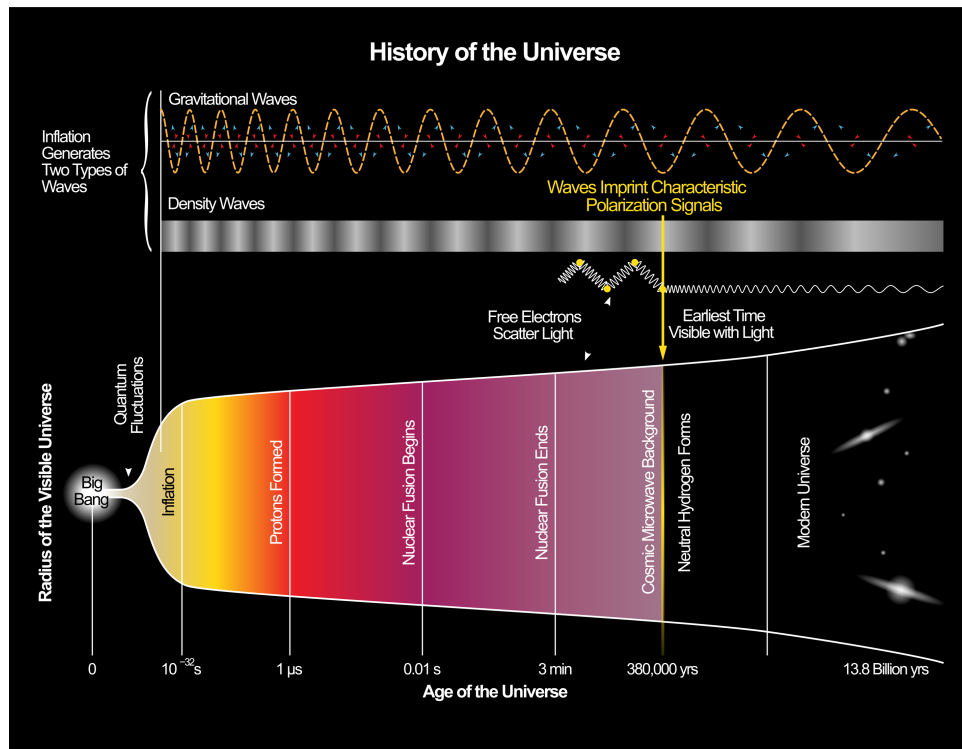
# The first 3 minutes of the Universe



Resolution of current instrumentation :  
 $1/1000$  of the size of a proton.



# The first 3 minutes of the Universe



$t=0$ s : the Big-Bang

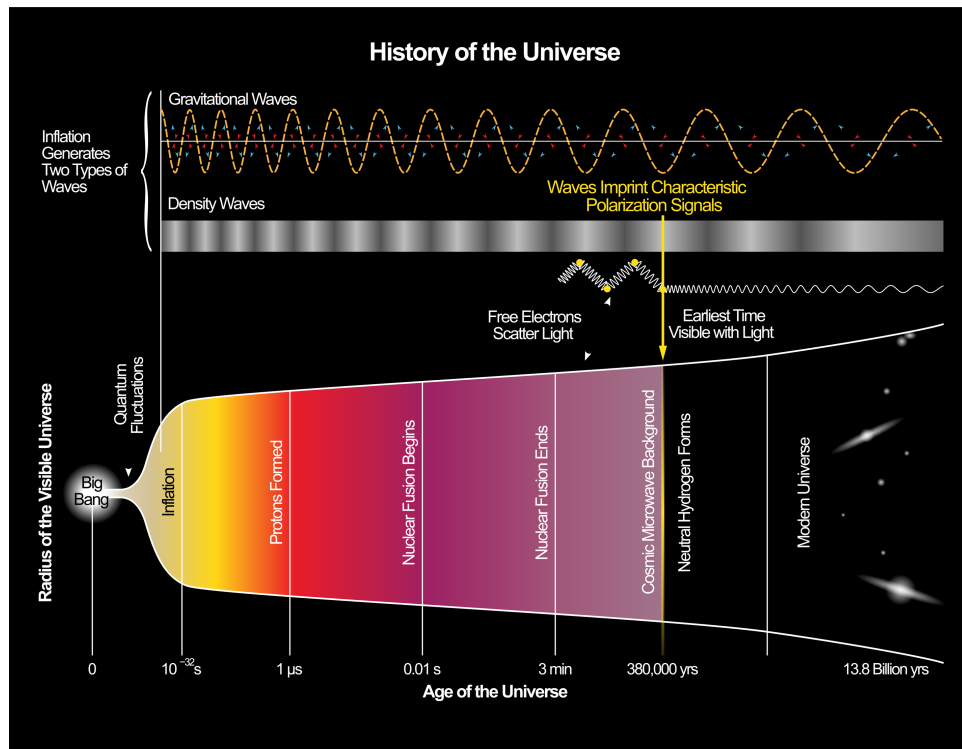
$t=10^{-36}$  to  $t=10^{-32}$ s : inflation

- emission of gravitational waves
- emission of density waves

Guzzetti et al. 2016, arXiv: 1605.01615

three generations of matter (fermions)			interactions / force carriers (bosons)	
I	II	III		
mass $\approx 2.2 \text{ MeV}/c^2$ charge $\frac{2}{3}$ spin $\frac{1}{2}$ <b>u</b> up	mass $\approx 1.28 \text{ GeV}/c^2$ charge $\frac{2}{3}$ spin $\frac{1}{2}$ <b>c</b> charm	mass $\approx 173.1 \text{ GeV}/c^2$ charge $\frac{2}{3}$ spin $\frac{1}{2}$ <b>t</b> top	mass 0 charge 0 spin 1 <b>g</b> gluon	mass $\approx 124.97 \text{ GeV}/c^2$ charge 0 spin 0 <b>H</b> higgs
mass $\approx 4.7 \text{ MeV}/c^2$ charge $-\frac{1}{3}$ spin $\frac{1}{2}$ <b>d</b> down	mass $\approx 96 \text{ MeV}/c^2$ charge $-\frac{1}{3}$ spin $\frac{1}{2}$ <b>s</b> strange	mass $\approx 4.18 \text{ GeV}/c^2$ charge $-\frac{1}{3}$ spin $\frac{1}{2}$ <b>b</b> bottom	mass 0 charge 0 spin 1 <b><math>\gamma</math></b> photon	<b>SCALAR BOSONS</b>
mass $\approx 0.511 \text{ MeV}/c^2$ charge -1 spin $\frac{1}{2}$ <b>e</b> electron	mass $\approx 105.66 \text{ MeV}/c^2$ charge -1 spin $\frac{1}{2}$ <b><math>\mu</math></b> muon	mass $\approx 1.7768 \text{ GeV}/c^2$ charge -1 spin $\frac{1}{2}$ <b><math>\tau</math></b> tau	mass $\approx 91.19 \text{ GeV}/c^2$ charge 0 spin 1 <b>Z</b> Z boson	
mass $< 1.0 \text{ eV}/c^2$ charge 0 spin $\frac{1}{2}$ <b><math>\nu_e</math></b> electron neutrino	mass $< 0.17 \text{ MeV}/c^2$ charge 0 spin $\frac{1}{2}$ <b><math>\nu_\mu</math></b> muon neutrino	mass $< 18.2 \text{ MeV}/c^2$ charge 0 spin $\frac{1}{2}$ <b><math>\nu_\tau</math></b> tau neutrino	mass $\approx 80.39 \text{ GeV}/c^2$ charge $\pm 1$ spin 1 <b>W</b> W boson	
<b>LEPTONS</b>			<b>GAUGE BOSONS VECTOR BOSONS</b>	

# The first 3 minutes of the Universe



**$t=0$ s : the Big-Bang**

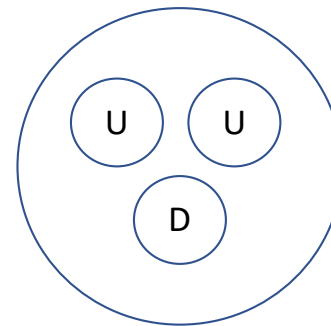
**$t=10^{-36}$  to  $t=10^{-32}$ s : inflation**

- emission of gravitational waves
- emission of density waves

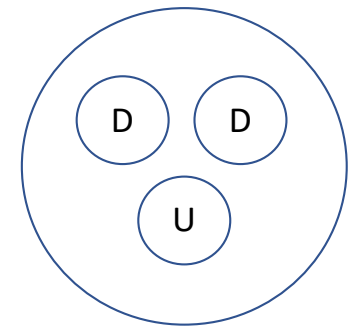
Guzzetti et al. 2016, arXiv: 1605.01615

- Universe mainly composed of quarks, leptons and photons

**$t=10^{-6}$ s : formation of protons and neutrons**

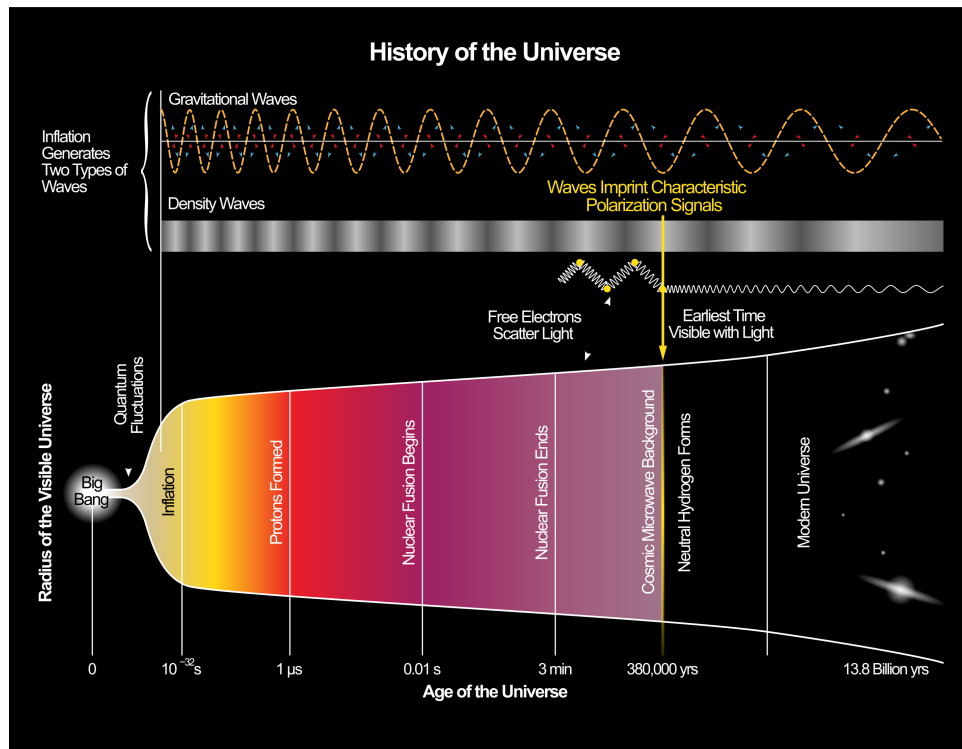


Proton



Neutron

# The first 3 minutes of the Universe



$t=0$ s : the Big-Bang

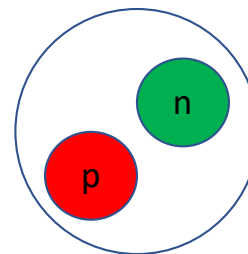
$t=10^{-36}$  to  $t=10^{-32}$ s : inflation

- emission of gravitational waves
- emission of density waves

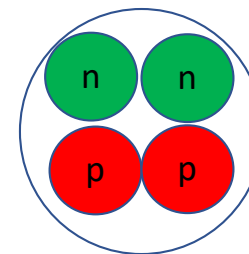
Guzzetti et al. 2016, arXiv: 1605.01615

- Universe mainly composed of quarks, leptons and photons

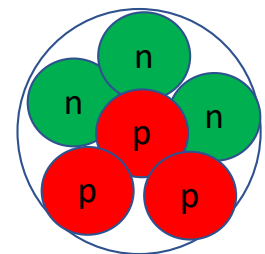
$t=10^{-6}$ s : formation of protons and neutrons, and then formation of nuclei of deuterium, helium and lithium



Deuterium

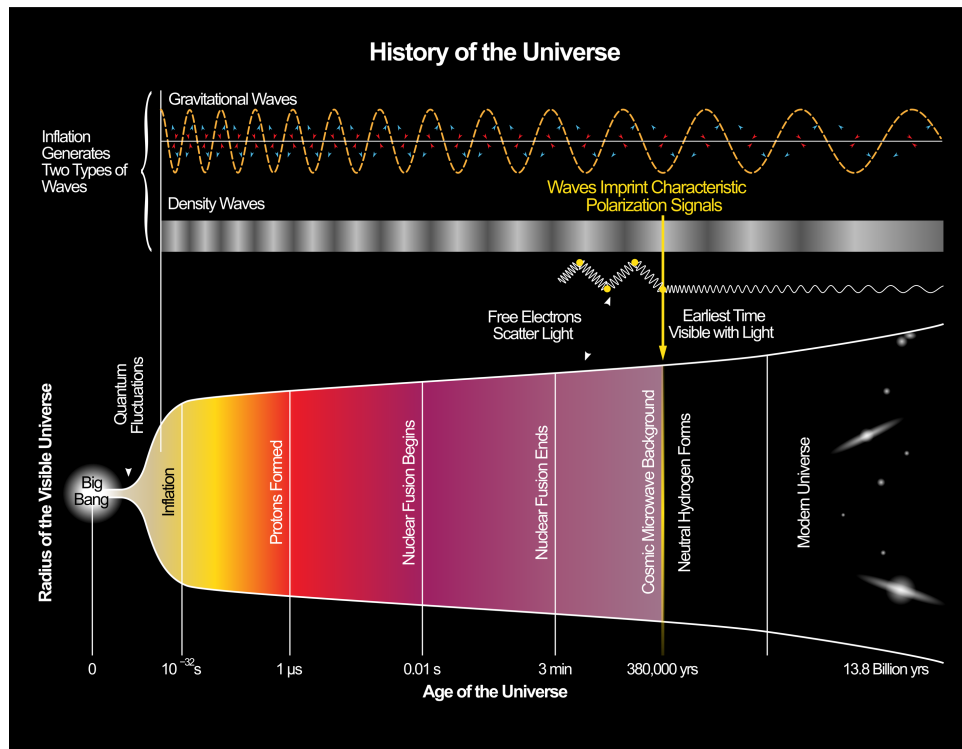


Helium



Lithium

# The first 3 minutes of the Universe



**$t=0s$  : the Big-Bang**

**$t=10^{-36}$  to  $t=10^{-32}s$  : inflation**

- emission of gravitational waves
- emission of density waves

Guzzetti et al. 2016, arXiv: 1605.01615

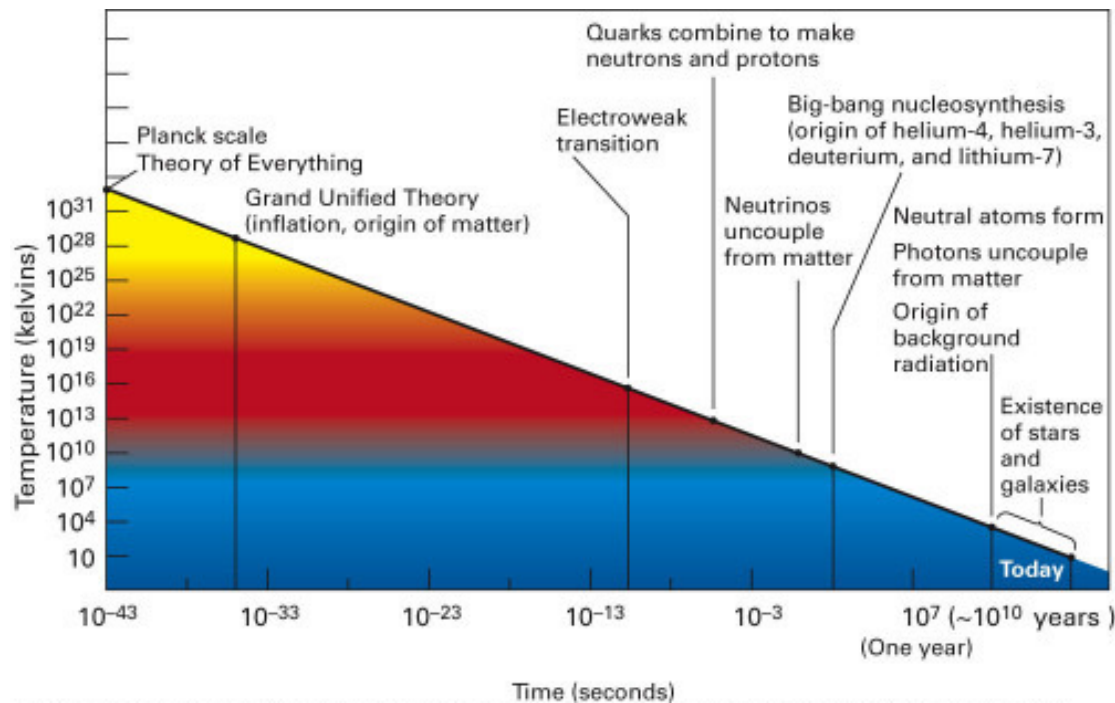
- Universe mainly composed of quarks, leptons and photons

**$t=10^{-6}s$  : formation of protons and neutrons, and then formation of nuclei of deuterium, helium and lithium.**

**$t=3mn$  : the Universe is mainly composed of radiation, baryonic matter, dark matter and dark energy.**

- *Electrons and nuclei are not bounded yet.*

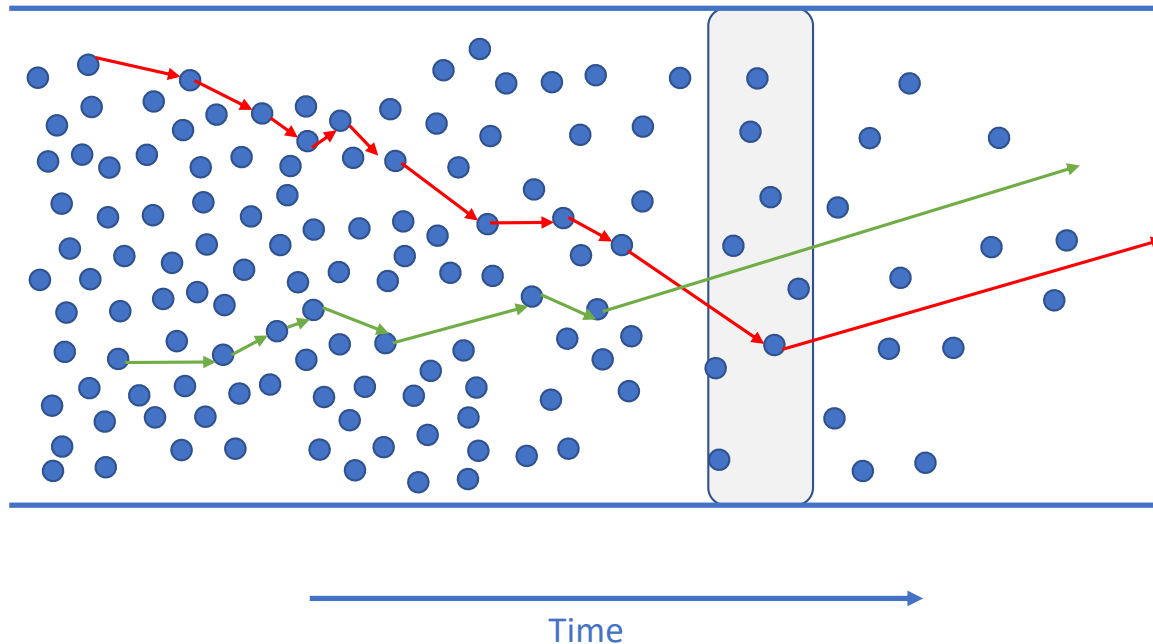
# The formation of the first stars and galaxies



- Over-dense regions grow from the initial perturbation
- As the Universe is expanding, the Universe's temperature is decreasing.
- The Universe's density is also decreasing as the Universe is expanding



# The formation of the first stars and galaxies



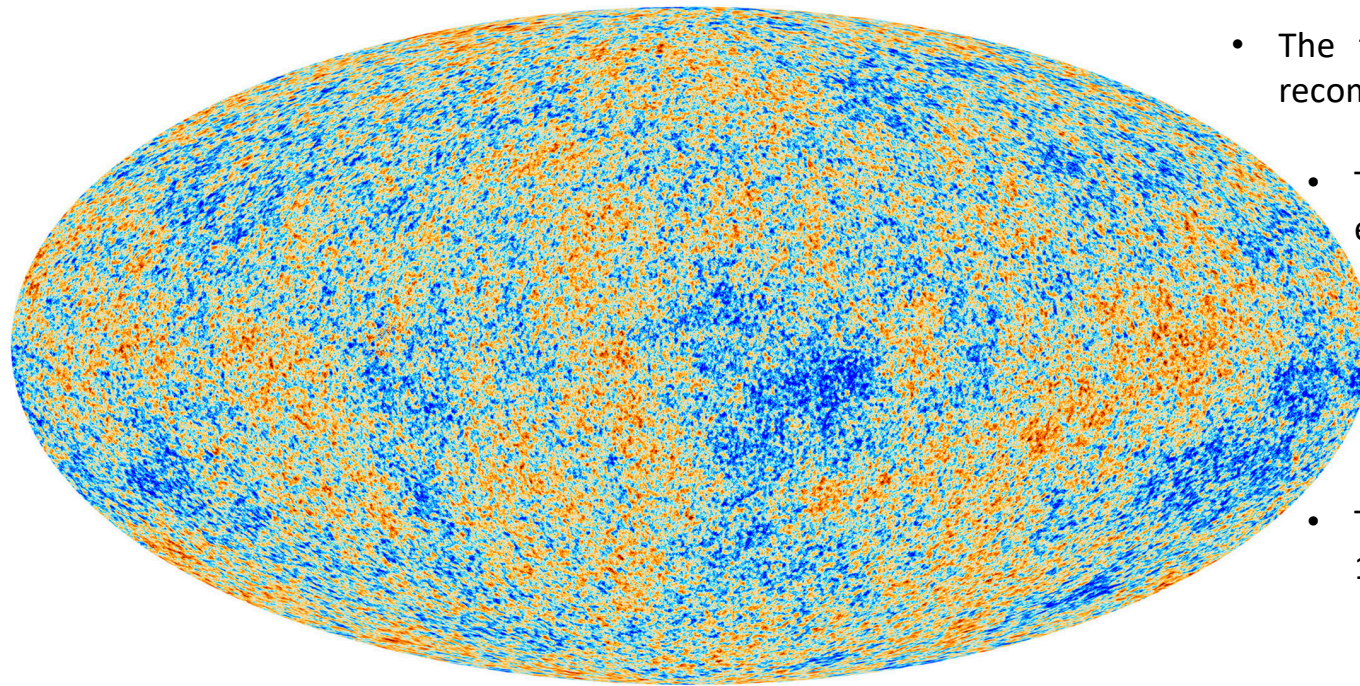
- Free electrons and protons start to be bounded but as soon as they are hit by a photon they become again unbounded :



- When the Universe's density is sufficiently low to avoid interaction between photons and particles (*matter and radiation are decoupled*) :
  - The first atoms are formed (Hydrogen, Helium, Lithium)
  - Photons can escape, and form the first emitted radiation in the Universe : the **Cosmic Microwave Background**

This epoch is called **the recombination phase**

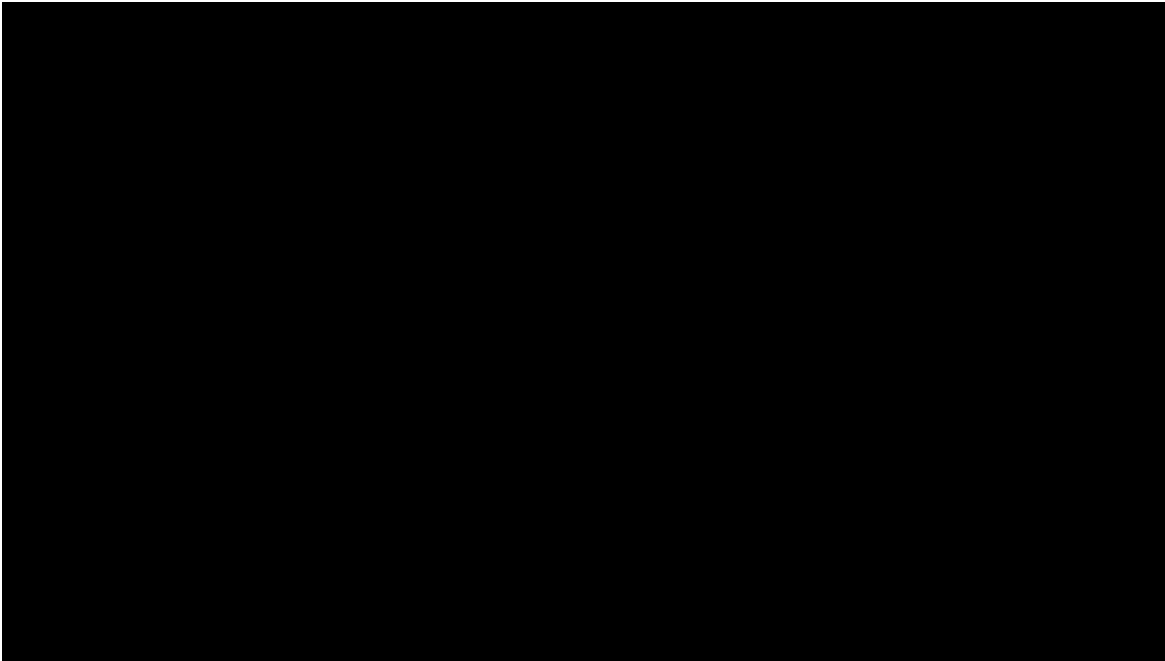
# The formation of the first stars and galaxies



-300  300  $\mu\text{K}$

- The temperature of the Universe at the recombination epoch was  $\sim 3000\text{K}$
- The redshift of the recombination epoch is  $z \sim 1100$
- Therefore, the observed temperature of the CMB is today :
$$T \approx \frac{3000}{1+z} = \frac{3000}{1101} \approx 2.7\text{ K}$$
- The CMB is observed at a frequency of 160.23 GHz

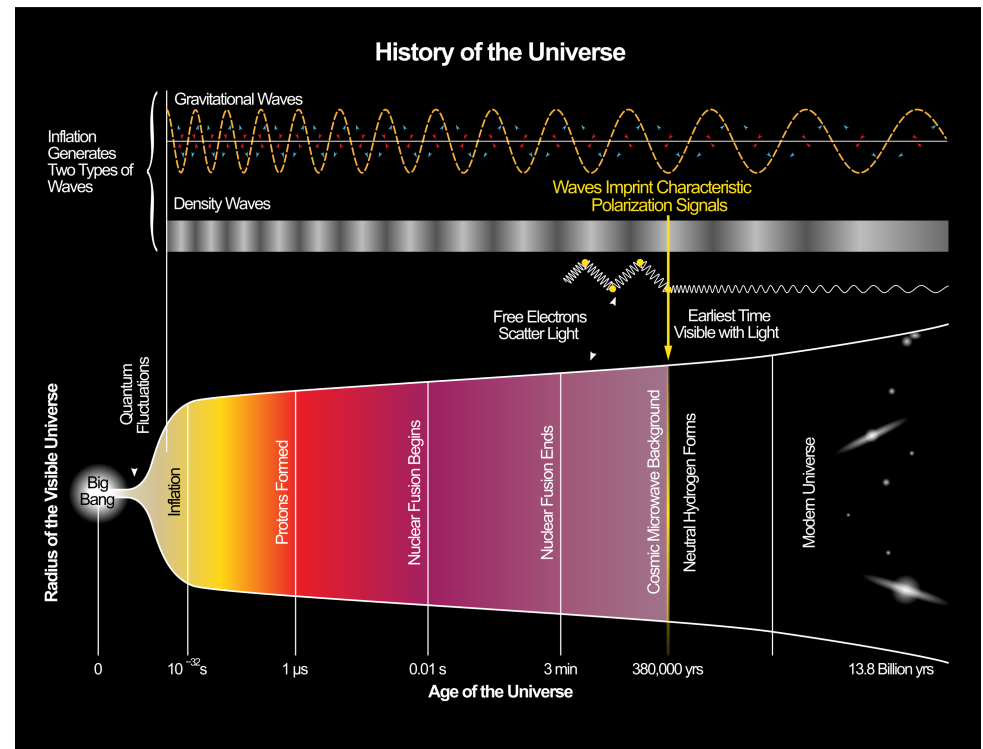
# The formation of the first stars and galaxies



- European Space Agency (ESA) satellite
- Launched by an Ariane 5 rocket in May 2009
- Diameter :1.5m
- Objectives :
  - Map the Cosmic Microwave Background
  - Measure the cosmological parameters
  - Study galaxy clusters

# The formation of the first stars and galaxies

- After the recombination phase, the Universe enters the **Dark Ages**
- Overdense regions continue to grow
- Their density becomes sufficiently large that their gravitational field is dominated by their own mass
- Their evolution is now driven by their own gravity (self-gravitating objects) and not the evolution of the Universe (Hubble flow)
- At the center of these overdense regions, the gas cools and leads to the formation of the first stars : this epoch is called **Cosmic Dawn**



# The formation of the first stars and galaxies

- The first stars are surrounded by neutral hydrogen
- The first stars emit UV photons\* which will ionise the neutral hydrogen, creating bubbles of ionised hydrogen : this is the **epoch of reionisation**



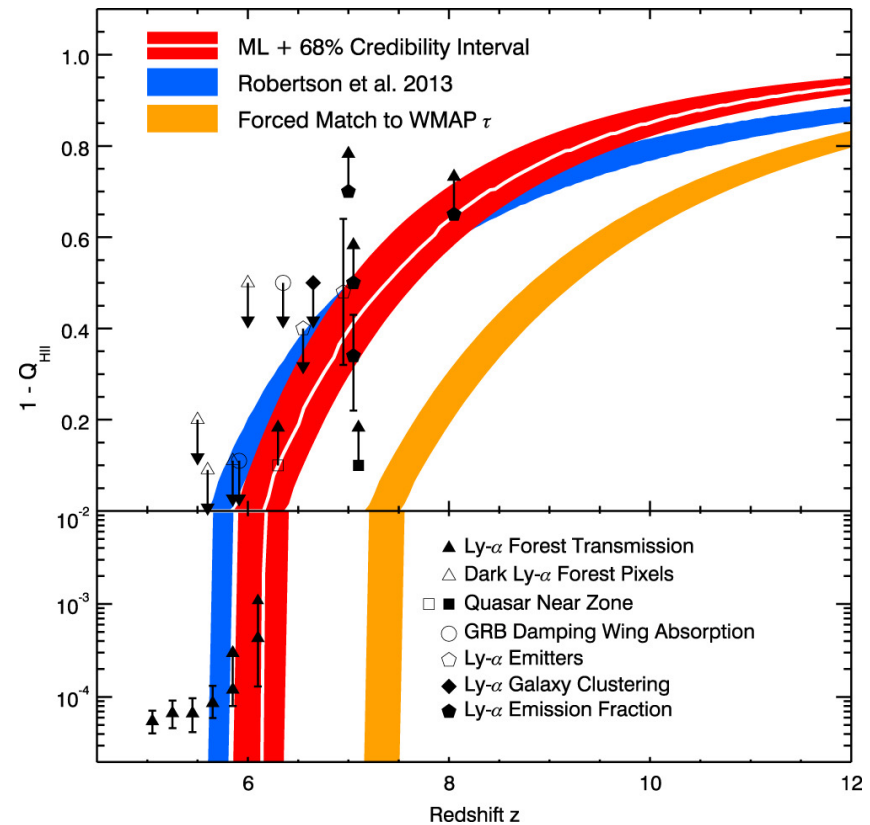
[www.eso.org](http://www.eso.org)

\* *This will be discussed later in this course*

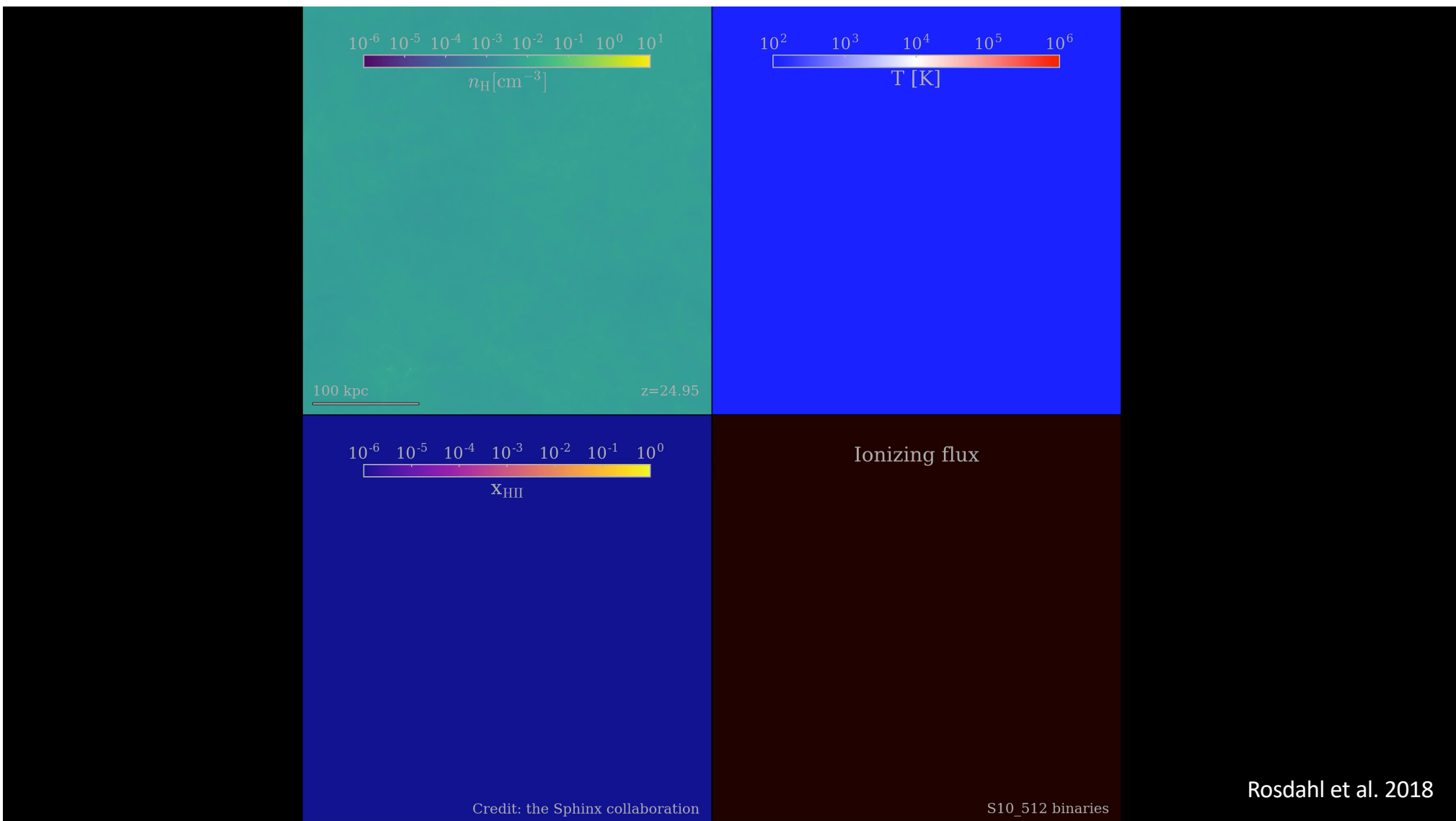


# The formation of the first stars and galaxies

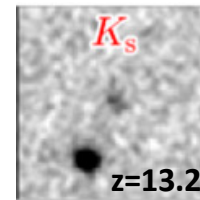
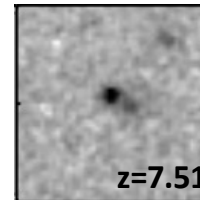
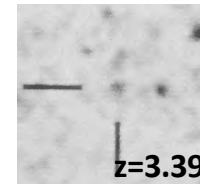
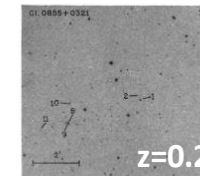
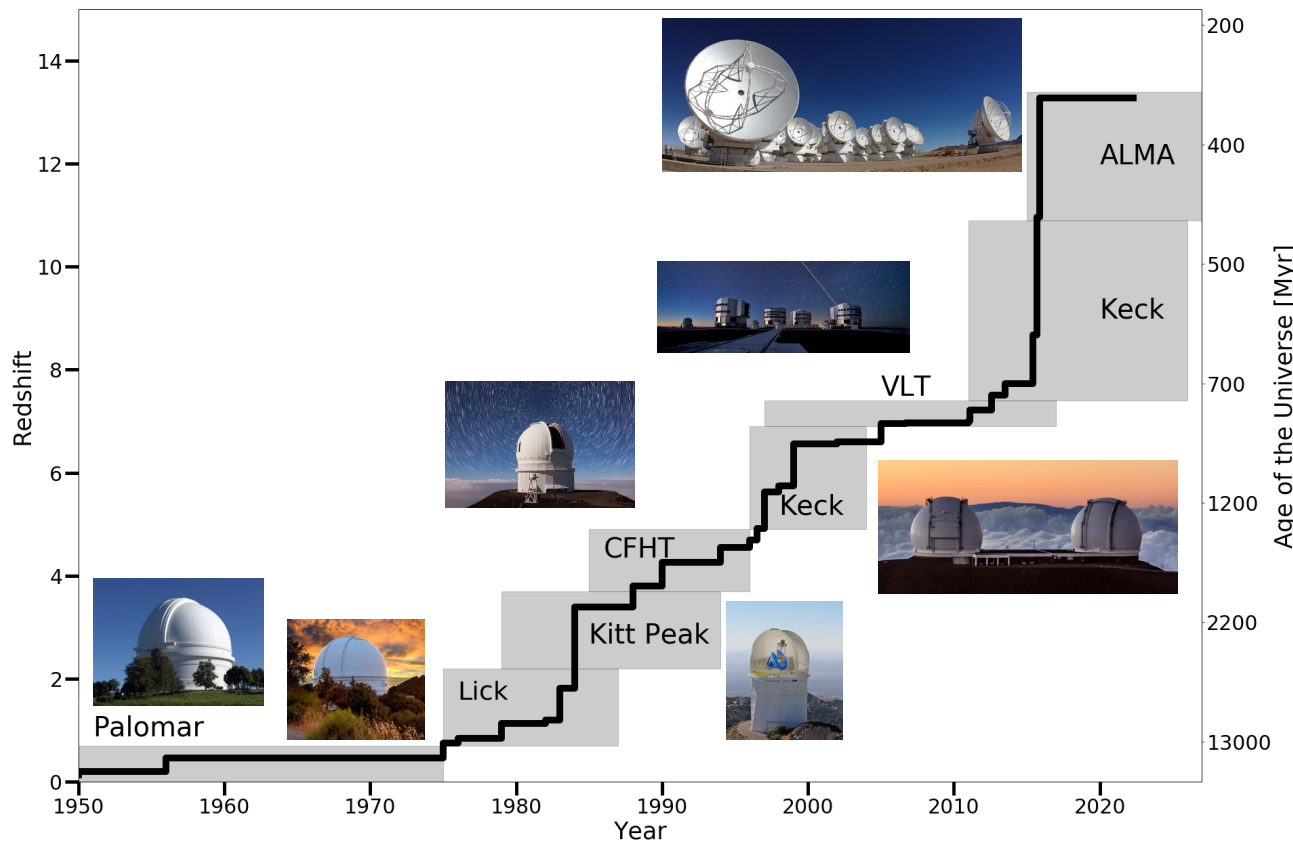
- The first stars are surrounded by neutral hydrogen
- The first stars emit UV photons\* which will ionise the neutral hydrogen, creating bubbles of ionised hydrogen : this is the **epoch of reionisation**
- CMB observations by *Planck* reveals that the hydrogen is fully ionised 1 billion years after the Big-Bang ( $z=6$ )
- The study of the first generation of galaxies shows that they grow hierarchically by merging, leading to an evolving distribution of galaxies of different masses.



\* This will be discussed later in this course



# The “hunt” for the most distant galaxies *between 1950s and 2022*

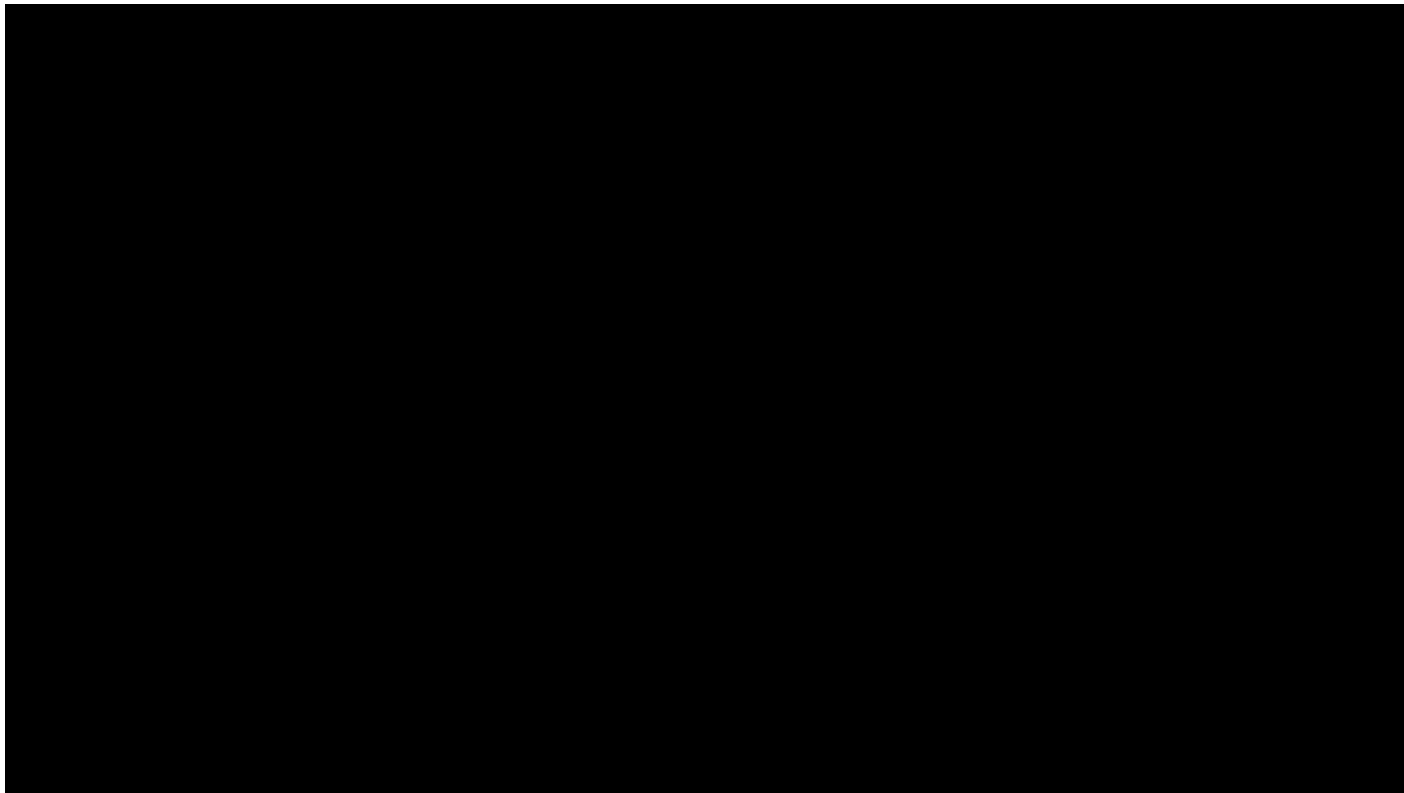


- Humason et al. 1956
- Minkowski 1960
- Spinrad et al. 1975
- Spinrad & Smith 1976
- Smith et al. 1979
- Spinrad 1982
- Spinrad & Djorgovsky 1984
- Lilly 1988
- Chambers et al. 1990
- Lacy et al. 1994
- Petitjean et al. 1996
- Franz et al. 1997
- Day et al. 1998
- Hu et al. 1999, 2002
- Pelló et al. 2004
- Iye et al. 2006
- Fontana et al. 2010
- Vanzella et al. 2011
- Ono et al. 2012
- Shibuya et al. 2012
- Finkelstein et al. 2013
- Oesch et al. 2014
- Zitrin et al. 2015
- Oesch et al. 2016
- Harikane et al. 2022

# The arrival of the *James Webb* Space Telescope

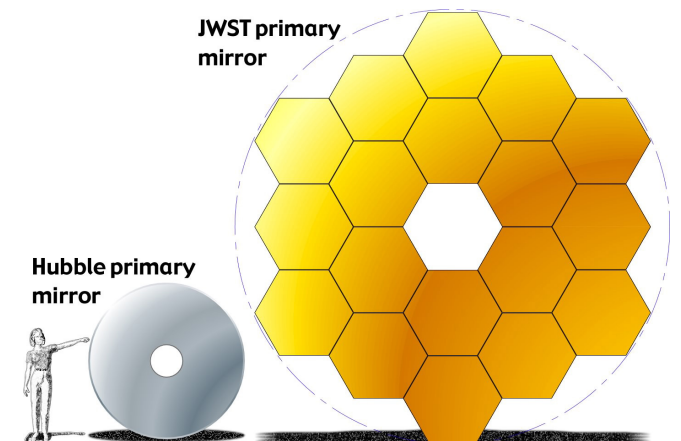
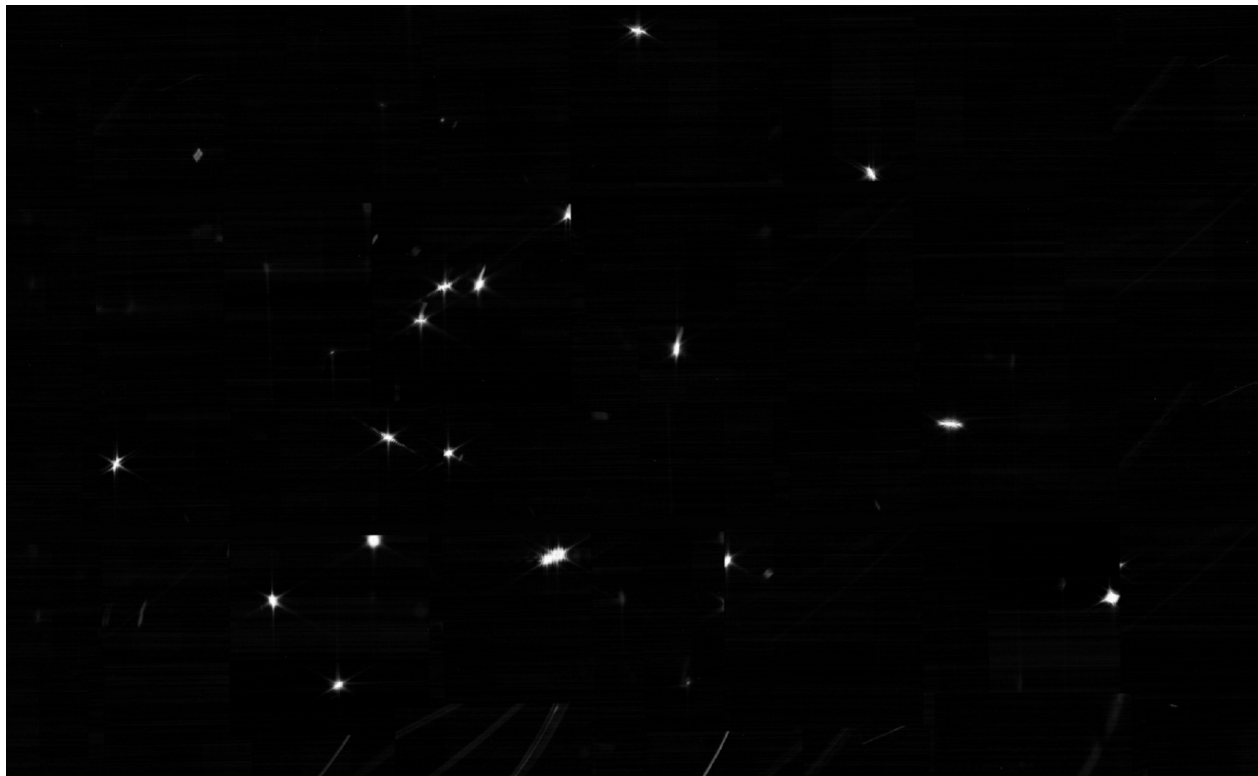


# The arrival of the *James Webb* Space Telescope

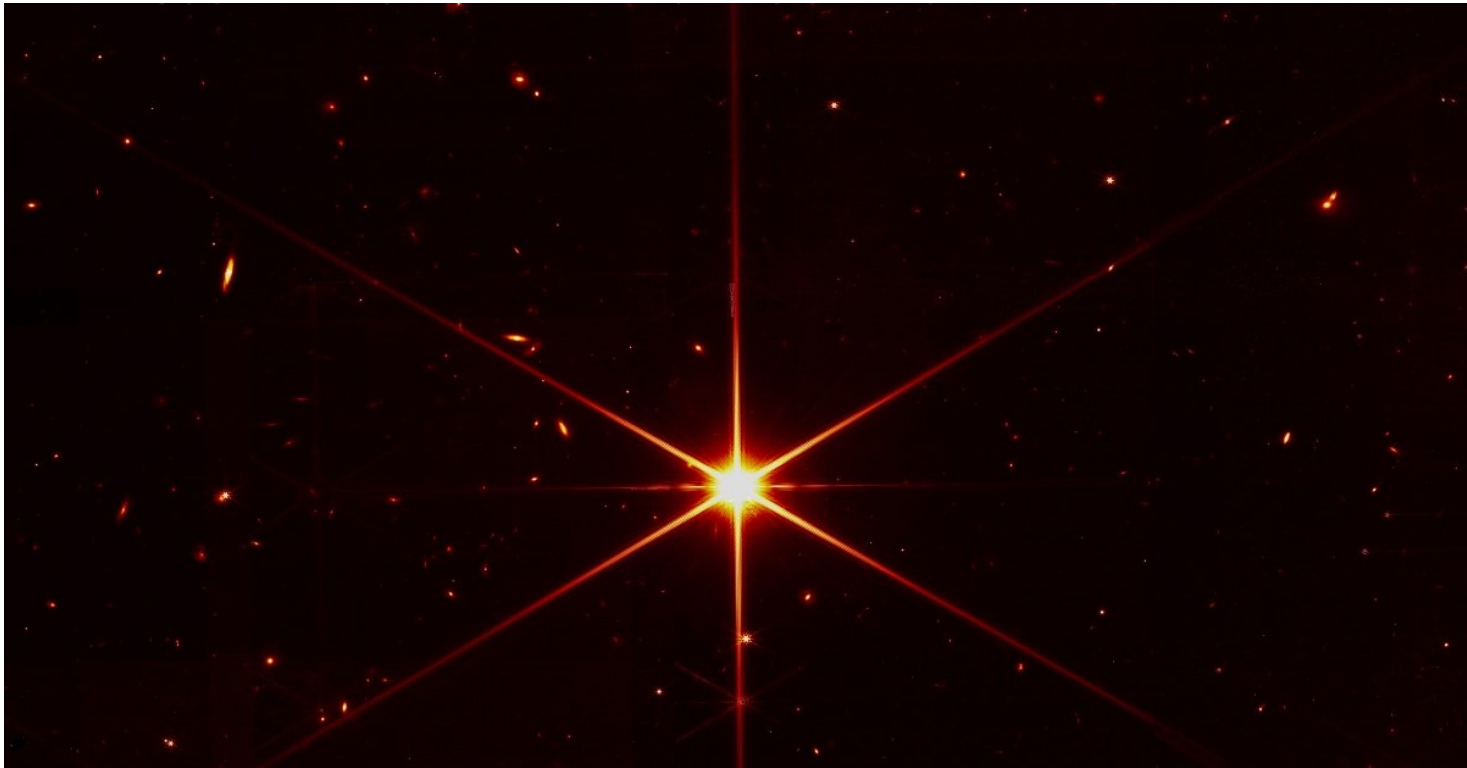




# The arrival of the *James Webb* Space Telescope



# The arrival of the *James Webb* Space Telescope



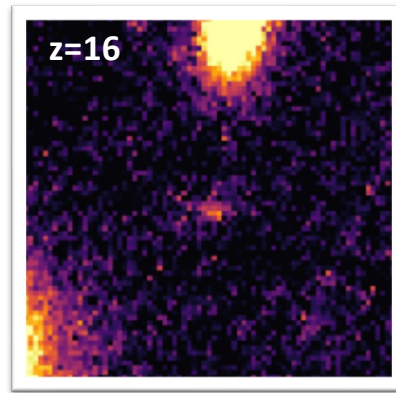
# The arrival of the *James Webb* Space Telescope



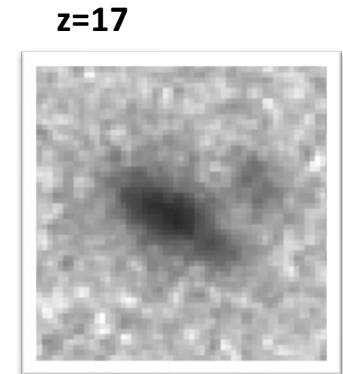
# The arrival of the *James Webb* Space Telescope



GLASS-z13 (Naidu et al. 2022)



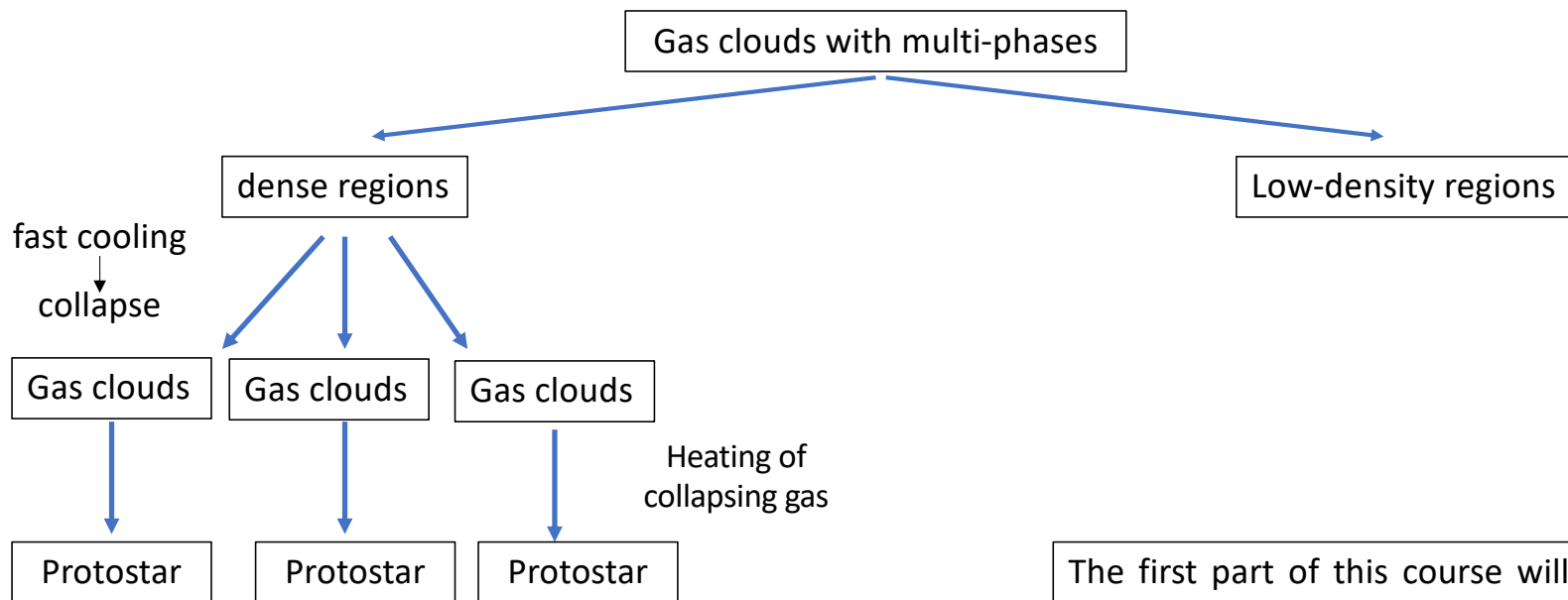
SMACS-z16a (Atek et al. 2022)



CEERS-DSFG-1 (Finkelstein et al. 2022)

Within a week, 11 papers have been submitted using the first dataset from the JWST to search for the first galaxies.

# Summary of the formation of structures in the Universe



The first part of this course will be to describe the processes responsible for the cooling of the gas, the heating of the gas and the formation of protostars.

# Toolbox for this course

## Euler's equation

*Adiabatic and inviscid flow*

$$\rho \frac{d\vec{v}}{dt} + \rho(\vec{v} \cdot \nabla)\vec{v} = -\nabla P - \rho \nabla \Phi_g$$

Annotations:

- Flow velocity (points to  $\vec{v}$ )
- pressure (points to  $P$ )
- Gravitational potential (points to  $\Phi_g$ )

## Equation of continuity

*Conservation of some quantities*

$$\frac{d\rho}{dt} + \nabla \cdot \vec{j} = 0$$

Annotations:

- Density (mass/unit volume) (points to  $\rho$ )
- Flux= $\rho\vec{v}$  (points to  $\vec{j}$ )

## Poisson's equation

*Differential equation*

$$\Delta \Phi = \nabla^2 \Phi = f$$

*For the gravitational potential we can write :*

$$\nabla^2 \Phi_g = 4\pi g \rho(\vec{r})$$

## Equation of state for an ideal gas

$$P = \frac{\rho k_B T}{\mu}$$

Annotation:

- Mass particle (points to  $\mu$ )





# Physical processes in baryonic gas

Chapter 2 (part 2)

# Some definitions

The amount of energy ( $dE$ ) passing through a surface should be proportional to the size of the surface ( $dA$ ) and to the duration of the exposition ( $dt$ ).

It is usually defined as :

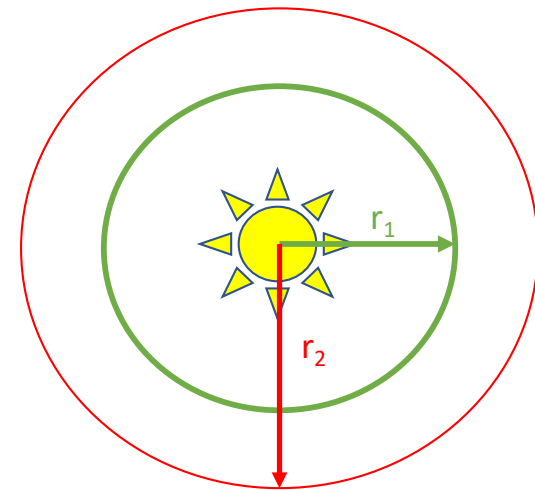
$$dE = dF \times dA \times dt$$

The energy flux  $dF$  is measured in  $\text{erg s}^{-1} \text{cm}^{-2}$

A source of radiation is isotropic if it emits energy equally in all directions

By conservation of Energy,  $dE(r_1) = dE(r_2)$  then :

$$F(r_1)4\pi r_1^2 = F(r_2)4\pi r_2^2$$



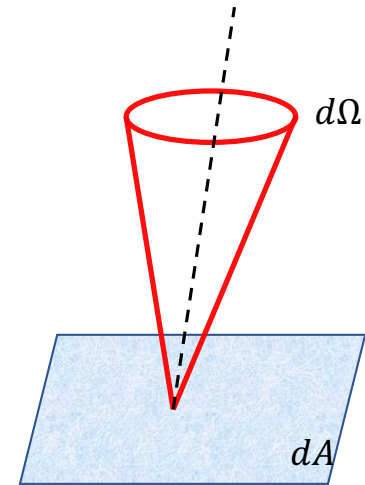
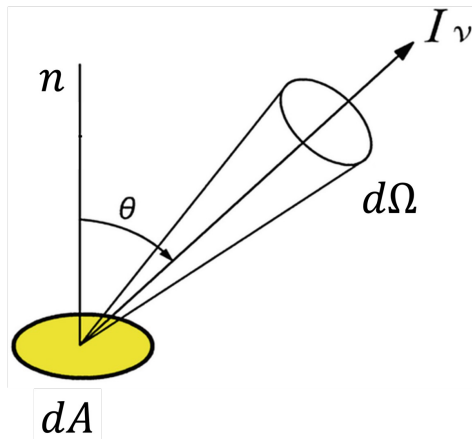
$$F(r) = \frac{F(r_1)r_1^2}{r^2}$$

# Some definitions

Considering a surface normal to the direction of a given ray, and considering all the rays whose direction is within a solid angle  $d\Omega$ , then the energy passing through the element  $dA$  is :

$$dE = I_\nu dA dt d\nu d\Omega$$

where  $I_\nu$  is the specific intensity (or brightness)



If the surface is not perpendicular to the rays but has different orientation, then

$$\begin{aligned} dE &= I_\nu dA dt d\nu \cos \theta d\Omega \\ &= dF_\nu dA dt d\nu \end{aligned}$$

N.B. : If the radiation is isotropic, then  $\int dF_\nu = 0$

# Some definitions

The specific energy density is the energy per unit volume per unit frequency range :

$$dE = u_\nu(\Omega) dV d\Omega d\nu$$

If we consider this cylinder, then  $dV = dA c dt$  then

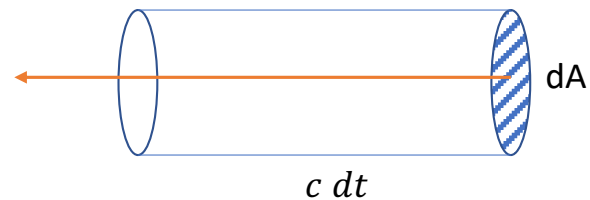
$$dE = u_\nu(\Omega) dA c dt d\Omega d\nu$$

but within  $dt$  all radiation will pass out of the cylinder, then :

$$dE = I_\nu dA d\Omega dt d\nu$$

The specific energy density is defined as :

$$u_\nu(\Omega) = \frac{I_\nu}{c}$$



Integrating the specific energy density over solid angles :

$$u_\nu = \int u_\nu(\Omega) d\Omega = \frac{1}{c} \int I_\nu d\Omega$$

$$\text{or } u_\nu = \frac{4\pi}{c} J_\nu$$

The mean density is defined as :

$$J_\nu = \frac{1}{4\pi} \int I_\nu d\Omega$$

The total radiation density is given by

$$u = \int u_\nu d\nu = \frac{4\pi}{c} \int J_\nu d\nu$$

# Radiative transfer

We use radiative transfer each time a radiation is passing through a matter and add (absorption) or subtract (emission) energy.

## I- EMISSION

The spontaneous emission coefficient is defined as the energy emitted per unit time per unit solid angle per unit volume, such as :

$$dE = j \, dV \, d\Omega \, dt$$

If the emission is monochromatic (e.g., an emission line), we can define a monochromatic emission coefficient :

$$dE = j_\nu dV \, d\Omega \, dt \, d\nu$$

If the emission is isotropic, then :

$$j_\nu = \frac{1}{4\pi} P_\nu$$

where  $P_\nu$  is the radiated power

We can also define the emissivity as the energy emitted per unit frequency per unit time per unit mass, and rewrite the transmitted energy in an isotropic emission as :

$$dE = \epsilon_\nu \rho \, dV \, dt \, d\nu \, \frac{d\Omega}{4\pi}$$

For an isotropic emission, the relation between the emission coefficient and the emissivity is given by :

$$j_\nu = \frac{\epsilon_\nu \rho}{4\pi}$$

Considering a beam of cross-section  $dA$  traveling through a volume  $dV = ds \times dA$ , then the energy added by spontaneous emission is :

$$dI_\nu = j_\nu \, ds$$

(Remember that  $dE = I_\nu \, dA \, dt \, d\nu \, d\Omega$ )

# Radiative transfer

We use radiative transfer each time a radiation is passing through a matter and add (absorption) or subtract (emission) energy.

## II- ABSORPTION

The absorption coefficient is defined as the loss of intensity in a beam as it travels a distance  $ds$  :

$$dI_\nu = -\alpha_\nu I_\nu ds$$

The absorption depends on the density of absorbers along the travel of a beam.

If we assume a random distribution of absorbers, each of them with a cross section  $\sigma_\nu$  and a density per unit volume  $n$ , then the effect of these absorbers on a radiation passing through  $dA$  within a solid angle  $d\Omega$  is :

$$dE = -dI_\nu dA dt d\Omega d\nu$$

$$\text{or : } dE = I_\nu (n dA ds \sigma_\nu) d\Omega dt d\nu$$

Therefore :

$$dI_\nu = -n \sigma_\nu I_\nu ds$$

We can rewrite the absorption coefficient such as :

$$\alpha_\nu = n \sigma_\nu$$

Usually,  $\alpha_\nu$  is defined with the opacity (also known as the mass absorption coefficient) such as :

$$\alpha_\nu = \rho \kappa_\nu$$